

\*\*This is a packet of extra problems. It is not comprehensive! \*\*

1) Use  $f(x) = x^2 - 2x + 1$  and  $g(x) = 2x - 5$  to answer the following questions.

A)  $f(-1)$

4

B)  $g(1/2)$

-4

C)  $f(g(3))$

0

D)  $g(f(-4))$

45

E)  $f(2-3a)$

$$\begin{aligned} &= (2-3a)^2 - 2(2-3a) + 1 \\ &= 4 - 12a + 9a^2 - 4 + 6a + 1 \\ &= 9a^2 - 6a + 1 \end{aligned}$$

F)  $\frac{g(x+h) - g(x)}{h}$

$$\begin{aligned} &= \frac{2(x+h) - 5 - [2x - 5]}{h} \\ &= \frac{2x + 2h - 5 - 2x + 5}{h} \\ &= 2 \end{aligned}$$

2) Use the table shown here to answer the following questions.

x	f(x)	g(x)	h(x)
-1	2	10	4
0	3	2	5
2	5	-1	7
4	-1	0	-2
5	0	7	-1
7	0	2	0

A)  $f(5)$  0

B)  $h(g(0))$  7

C)  $f(h(2))$  0

D)  $g(f(4))$  10

E)  $f^{-1}(5)$  2

F)  $h^{-1}(7)$  2

3) Determine whether the functions below are inverses or not. Show all work to support your answer.

$$q(x) = \frac{2x-1}{4-x} \quad p(x) = \frac{4x+1}{x+2}$$

$$\begin{aligned} q(p(x)) &= \frac{2\left(\frac{4x+1}{x+2}\right) - 1}{4 - \frac{4x+1}{x+2}} \\ &= \frac{8x+2-x-2}{4x+8-4x-1} \\ &= \frac{7x}{7} = x \quad \checkmark \end{aligned}$$

$$\begin{aligned} p(q(x)) &= \frac{4\left(\frac{2x-1}{4-x}\right) + 1}{\frac{2x-1}{4-x} + 2} \\ &= \frac{8x-4+4-x}{2x-1+8-2x} \\ &= \frac{7x}{7} \\ &= x \quad \checkmark \end{aligned}$$

The composition = x so they are inverses!

4) Graph  $f(x)$ , determine the domain and range of  $f$ , find  $f^{-1}$ , and graph  $f^{-1}$

A)  $f(x) = \sqrt{x+2} - 5$

$\mathcal{D}$  of  $f$ :  $[-2, \infty)$

$$x = \sqrt{y+2} - 5$$

$$(x+5)^2 = y+2$$

$$y = (x+5)^2 - 2$$

$$f^{-1}(x) = (x+5)^2 - 2, x \geq -5$$

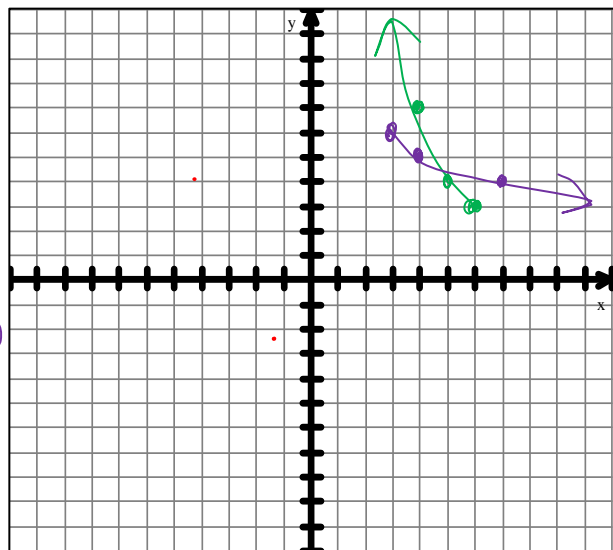
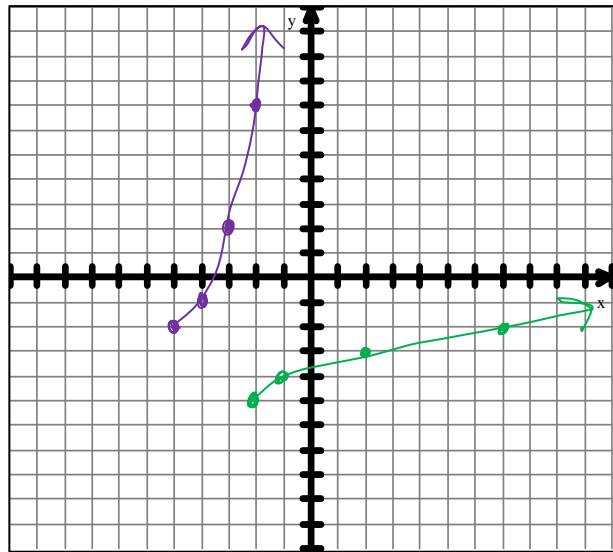
B)  $y = (x-6)^2 + 3, x \leq 6$

$\mathcal{D}$  of  $f$ :  $(-\infty, 6]$

$$x = (y-3)^2 + 6$$

$$\pm\sqrt{x-6} = y-3$$

$$f^{-1}(x) = -\sqrt{x-6} + 6, x \geq 6$$



5) Write the equation of a parabola in standard form with vertex  $(-2, 5)$  and pass through  $(6, 3)$ .

$$3 = a(b - (-2))^2 + 5$$

$$3 = a(6 + 2)^2 + 5$$

$$-2 = 64a$$

$$y = -\frac{1}{32}(x+2)^2 + 5$$

$$= -\frac{1}{32}(x^2 + 4x + 4) + 5$$

$$\frac{1}{32}x^2 - \frac{1}{8}x + \frac{39}{8}$$

6) Write the equation of a parabola passing through  $(0, -2)$ ,  $(2, -4)$ , and  $(3, -14)$ .

$$-2 = a(0)^2 + b(0) + c$$

$$-4 = a(2)^2 + b(2) + c$$

$$-14 = a(3)^2 + b(3) + c$$

$$y = -3x^2 + 5x - 2$$

7) Transform each equation to vertex form by completing the square.

A)  $y = -3x^2 + 6x - 2$

$$y = -3(x^2 - 2x) - 2$$

$$= -3(x^2 - 2x + 1) - 2 + 3$$

$$= -3(x-1)^2 + 1$$

B)  $y = \frac{1}{2}x^2 - 7x + 13$

$$y = \frac{1}{2}(x^2 - 14x) + 13$$

$$= \frac{1}{2}(x^2 - 14x + 49) + 13 - \frac{49}{2}$$

$$= \frac{1}{2}(x-7)^2 - \frac{23}{2}$$

8) Graph the quadratic equation with at least 5 points.

$$g(x) = -3x^2 - 6x + 5$$

$$x = \frac{b}{-a} = -1$$

Axis of symmetry:  $x = -1$

Vertex:  $(-1, 8)$

Domain:  $(-\infty, \infty)$

Range:  $(-\infty, 8]$

Interval for increasing:  $(-\infty, -1]$

Interval for decreasing:  $[-1, \infty)$

x-intercepts (approx. nearest tenth):  $-2.2, .8$

y-intercept:  $(0, 5)$

