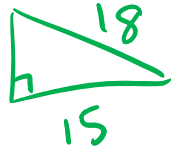
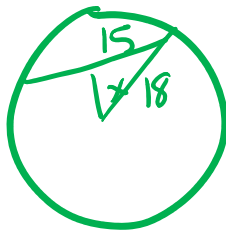
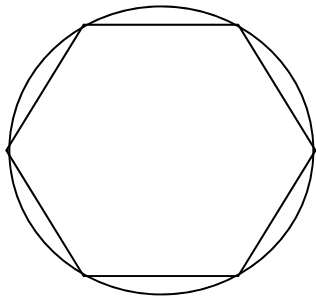


1. Find the distance from the center of a circle to a chord 30 m long if the diameter of the circle is 36 m.



$$3\sqrt{11}$$

2. A regular hexagon with a perimeter of 30 is inscribed in a circle. How far from the center is each side?



$$2.5\sqrt{3}$$

3. What is the length of the radius of a circle if a 30 degree arc has a length of 3π ?

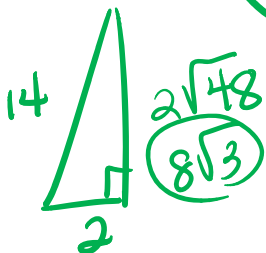
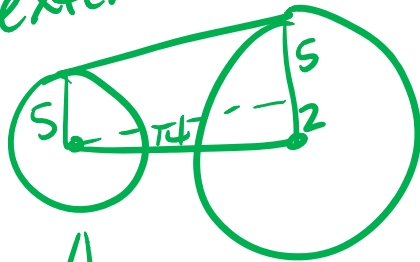
$$\frac{30}{360} = \frac{1}{12}$$

$$C = 36\pi$$

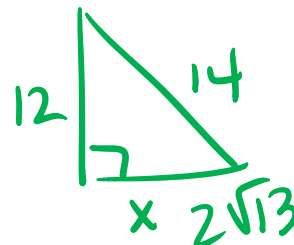
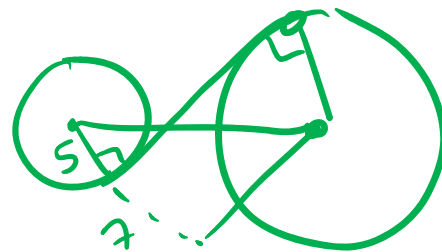
$$r = 18$$

4. Find the common external and internal tangents of two circles with radii of 5 and 7 if the centers are 14 units apart.

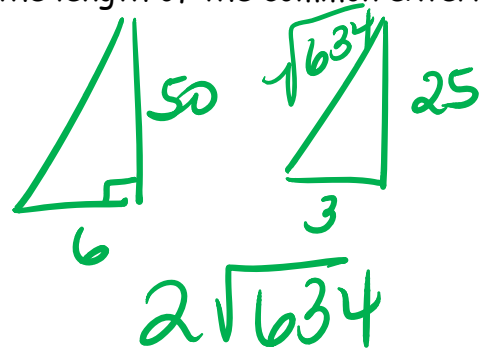
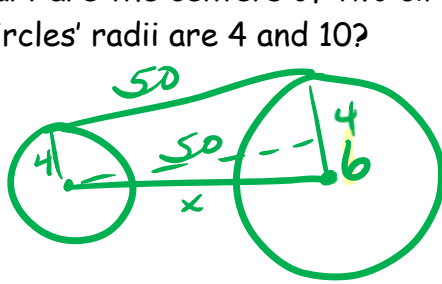
$$\text{Common external} = 8\sqrt{3}$$



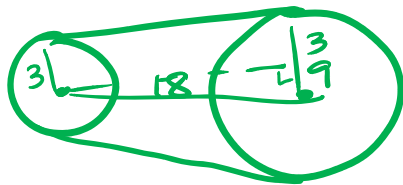
$$\text{Common internal} = 2\sqrt{13}$$



5. How far apart are the centers of two circles if the length of the common external tangent is 50, and the circles' radii are 4 and 10?



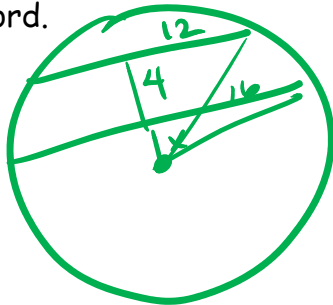
6. Find the length of a belt that is wrapped around two wheels of radii 3 cm and 12 cm if the distance between the centers of the wheels is 18 cm.



$$18\sqrt{3} + \frac{1}{3} \cdot 6\pi + \frac{2}{3} \cdot 24\pi$$

$$18\sqrt{3} + 18\pi$$

7. Find the radius of a circle in which a 32 cm chord is 4 cm closer to the center of the circle than a 24 cm chord.



$$r^2 = 16^2 + x^2$$

$$r^2 = (x+4)^2 + 12^2$$

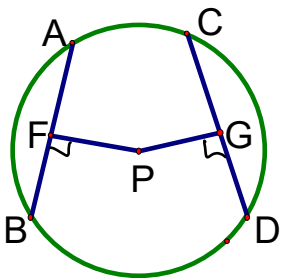
$$256 + x^2 = x^2 + 8x + 16 + 144$$

$$96 = 8x$$

$$12 = x$$

$$r = 20$$

8. $AB = \sqrt{4x+8}$, $DC = 2x+4$, $FP = GP$, P is the center of the circle. Find GD.



$$4x+8 = 4x^2 + 16x + 16$$

$$4x^2 + 12x + 8 = 0$$

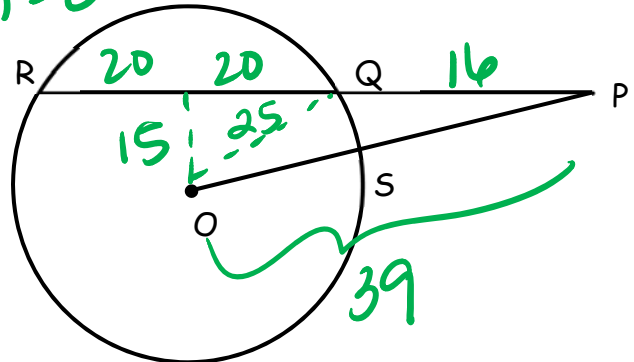
$$4(x^2 + 3x + 2) = 0$$

$$4(x+1)(x+2) = 0$$

$$x = -1, -2$$

$$GD = 1$$

9. Given: Circle O
 $PQ = 16$, $RQ = 40$, and $PO = 39$



Find: PS

$$PS = 14$$