

perfect cubes:

$$2^3 = 8 \quad 4^3 = 64 \quad 3^3 = 27$$

$$5^3 = 125 \quad 6^3 = 216 \quad 10^3 = 1000$$

Solve for x:

1. $4^3 = x$ 64

2. $6^3 = x$ 216

3. $10^3 = x$ 1000

4. $2^3 = x$ 8

5. $x^3 = 125$ 5

6. $x^3 = 27$ 3

7. $x^3 = -216$ -6

8. $x^3 = -8$ -2

9. $x^3 = -64$ -4

$$\begin{aligned} \text{Expand: } (x+2)(x^2 - 2x + 4) &= x^3 - 2x^2 + 4x + 2x^2 - 4x + 8 \\ &= x^3 + 8 \end{aligned}$$

$$x^3 + 8 = (x+2)(x^2 - 2x + 4)$$

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$$x^3 - 64 = (x-4)(x^2 + 4x + 16)$$

Sum and difference of perfect cubes.

Factor $x^3 + 8$.

Factor $x^3 - 125$.

$$(x - 5)(x^2 + 5x + 25)$$

$$x^{18} - 125y^{30} = (x^6)^3 - (5y^{10})^3$$

$$= (x^6 - 5y^{10})(x^{12} + 5x^6y^{10} + 25y^{20})$$

Factor $x^{12} + y^{24}$.

Factor completely:

① $a^3 + b^3$

$(a+b)(a^2 - ab + b^2)$

② $a^3 - b^3$

$(a-b)(a^2 + ab + b^2)$

③ $z^3 + 64$

$(z+4)(z^2 - 4z + 16)$

$$(4) \quad 64 - z^3$$
$$(4-z)(16+4z+z^2)$$

$$(5) \quad x^{18} - y^{24}$$
$$(x^6)^3 - (y^8)^3$$
$$= (x^6 - y^8)(x^{12} + x^6y^8 + y^{16})$$

$$(6) \quad 125x^3y^6 + 27z^9$$
$$(5xy^2)^3 + (3z^3)^3$$
$$= (5xy^2 + 3z^3)(25x^2y^4 - 15xy^2z^3 + 9z^6)$$

Factor by grouping:

$$x^3 + 5x^2 - 4x - 20$$

$$x^2(x+5) - 4(x+5)$$

$$(x+5)(x^2-4)$$

$$\star (x+5)(x-2)(x+2)$$

$$x^3 - 4x + 5x^2 - 20$$

$$x(x^2-4) + 5(x^2-4)$$

$$(x^2-4)(x+5)$$

$$(x-2)(x+2)(x+5)$$

You try:

$$(7) \quad 2x^3 - 6x^2 + 6x - 18$$

$$(8) \quad x^3 + 4x^2 - 9x - 36$$