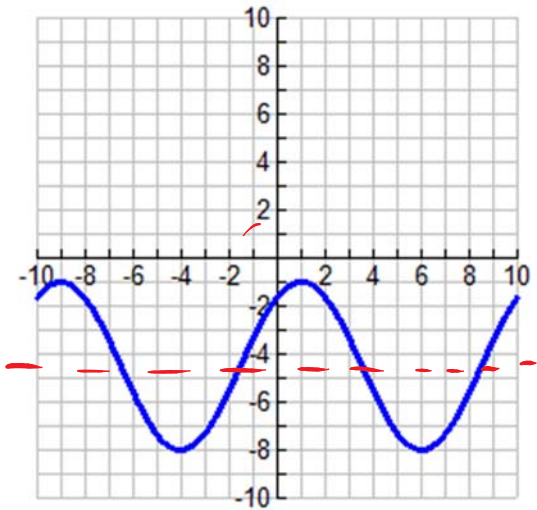


## 6.5 Transformations Summary and Writing Equations

1. Write four different equations transforming  $\sin\theta$  and  $\cos\theta$ .



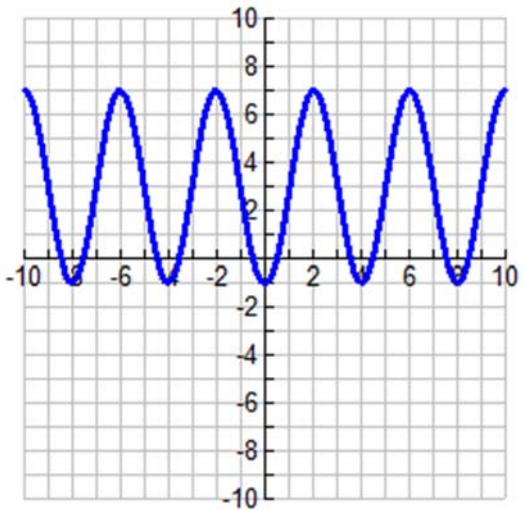
$$y = 3.5 \cos\left(\frac{\pi}{5}(x+9)\right) - 4.5$$

$$y = -3.5 \cos\left(\frac{\pi}{5}(x+4)\right) - 4.5$$

$$y = 3.5 \sin\left(\frac{\pi}{5}(x+1.5)\right) - 4.5$$

$$y = -3.5 \sin\left(\frac{\pi}{5}(x+6.5)\right) - 4.5$$

2. Write four different equations transforming  $\sin\theta$  and  $\cos\theta$ .



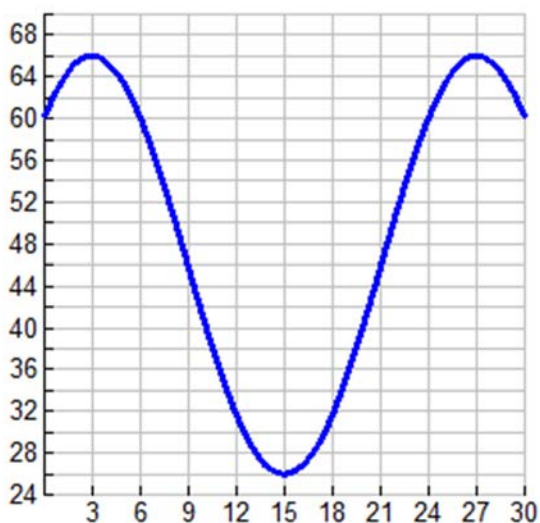
$$y = 4 \cos\left(\frac{\pi}{2}(x+2)\right) + 3$$

$$y = -4 \cos\left(\frac{\pi}{2}(x)\right) + 3$$

$$y = 4 \sin\left(\frac{\pi}{2}(x-1)\right) + 3$$

$$y = -4 \sin\left(\frac{\pi}{2}(x-3)\right) + 3$$

3. Write four different equations transforming  $\sin\theta$  and  $\cos\theta$ .



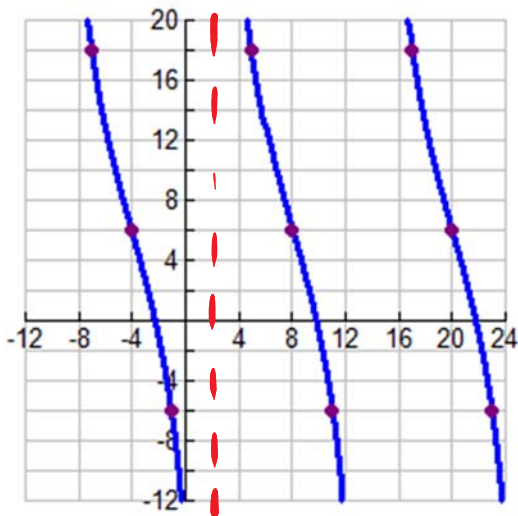
$$y = 20 \cos\left(\frac{\pi}{12}(x-3)\right) + 46$$

$$y = -20 \cos\left(\frac{\pi}{12}(x-15)\right) + 46$$

$$y = 20 \sin\left(\frac{\pi}{12}(x-21)\right) + 46$$

$$y = -20 \sin\left(\frac{\pi}{12}(x-9)\right) + 46$$

4. Write four different equations transforming  $\tan\theta$  and  $\cot\theta$ .



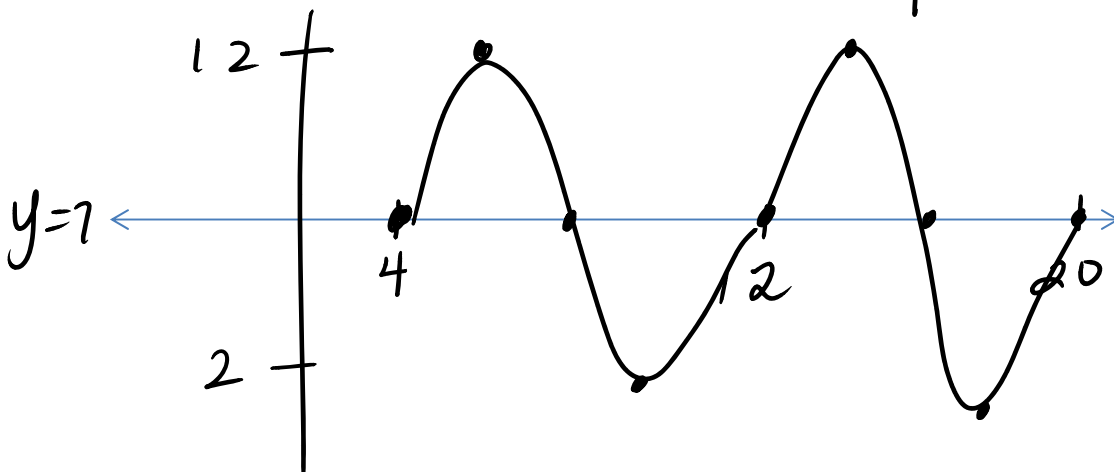
$$y = 12 \cot\left(\frac{\pi}{12}(x-2)\right) + 6$$

$$y = 12 \cot\left(\frac{\pi}{12}(x+10)\right) + 6$$

$$y = -12 \tan\left(\frac{\pi}{12}(x-8)\right) + 6$$

$$y = -12 \tan\left(\frac{\pi}{12}(x+4)\right) + 6$$

5. Graph two periods  $y = 5 \sin\left(\frac{\pi\theta}{4} - \pi\right) + 7 = 5 \sin\left(\frac{\pi}{4}(\theta - 4)\right) + 7$



Amplitude: 5

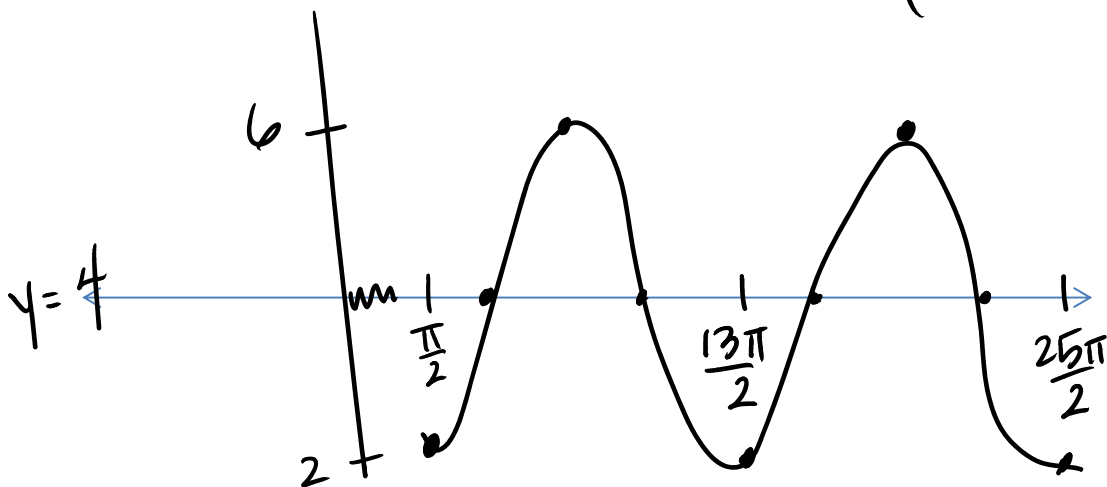
Sinusoidal axis:  $y = 7$

Period:  $2\pi \cdot \frac{4}{\pi} = 8$

Phase shift:  $4 \frac{\pi}{\pi} = 4$

End critical point: 12

6. Graph two periods  $y = -2 \cos\left(\frac{\theta}{3} - \frac{\pi}{6}\right) + 4 = -2 \cos\left(\frac{1}{3}\left(\theta - \frac{\pi}{2}\right)\right) + 4$



Amplitude: 2

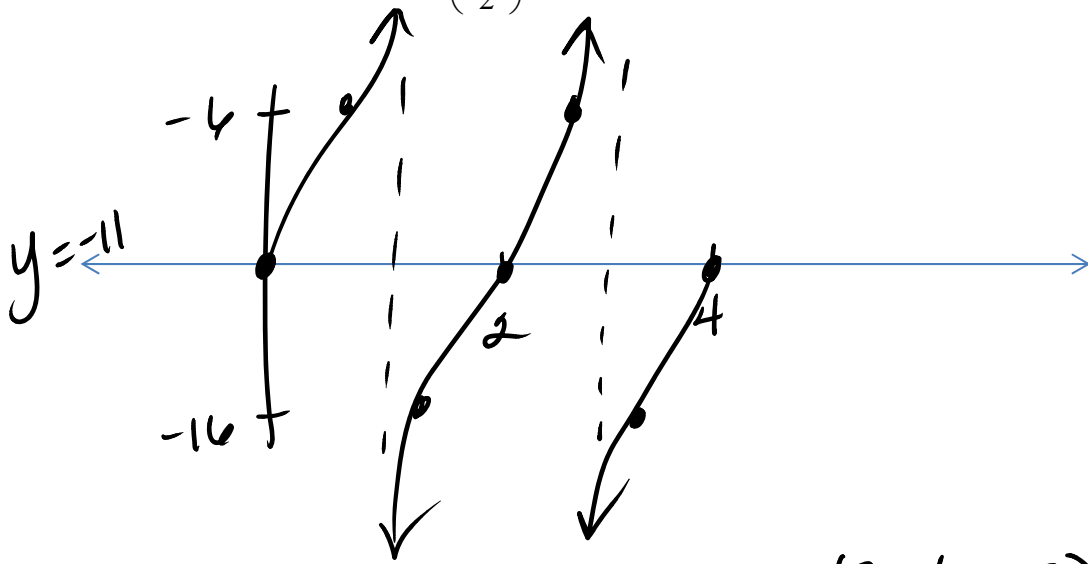
Sinusoidal axis:  $y = 4$

Period:  $2\pi \cdot 3 = 6\pi$

Phase shift:  $\frac{\pi}{2}$

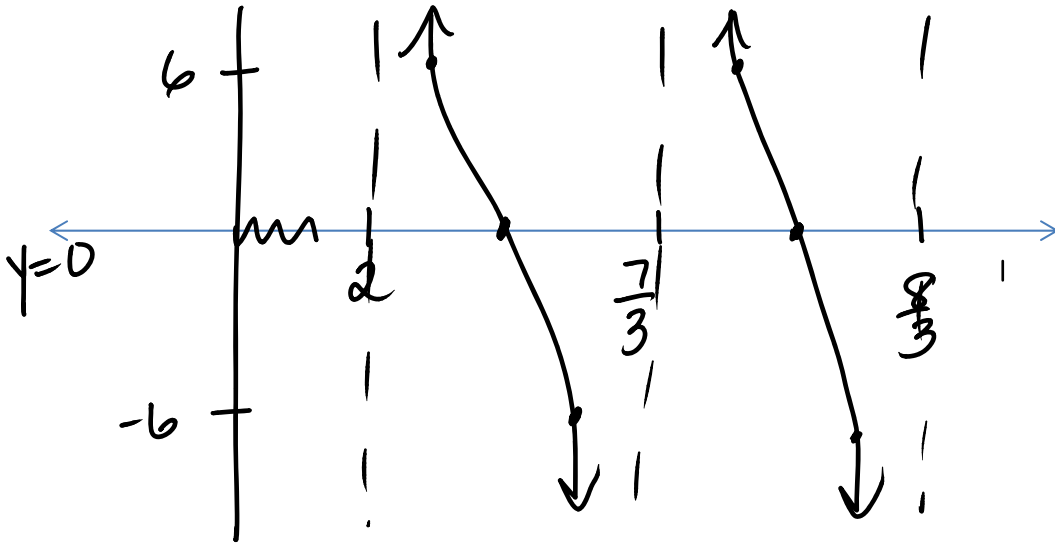
End critical point:  $13\pi/2$

7. Graph two periods  $y = 5 \tan\left(\frac{\pi\theta}{2}\right) - 11$



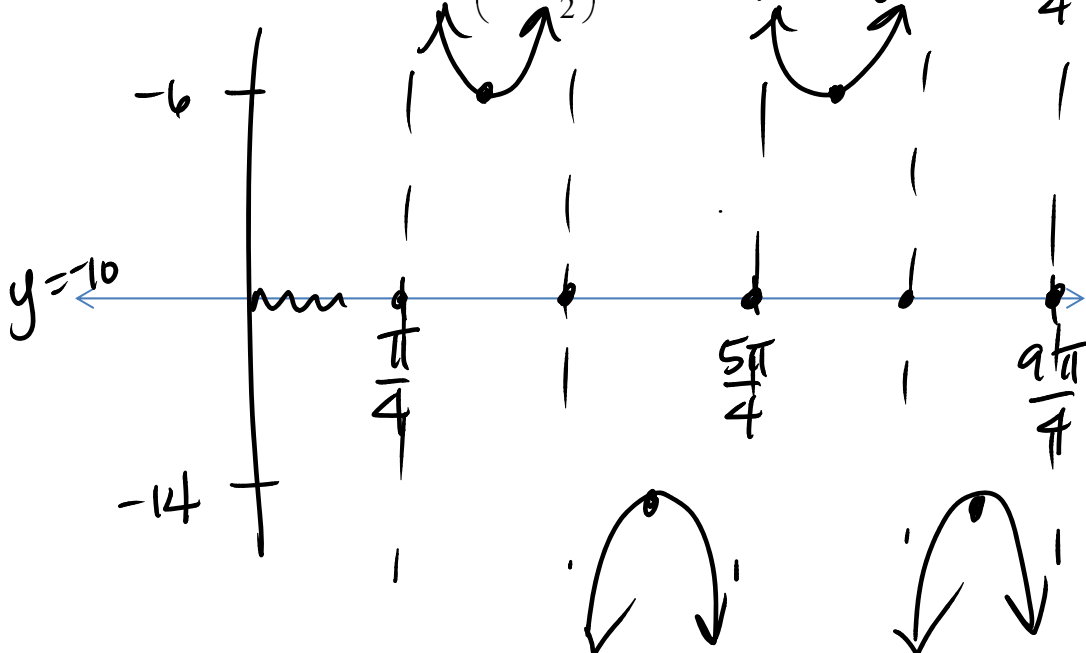
Midline:  $y = -11$   
 Period:  $\pi \cdot \frac{2}{\pi} = 2$   
 Phase shift: none  
 End critical point: 2

8. Graph two periods  $y = 6 \cot(3\pi\theta - 6\pi) = 6 \cot(3\pi(\theta - 2))$



Midline:  $y = 0$   
 Period:  $\frac{\pi}{3\pi} = \frac{1}{3}$   
 Phase shift: 2  
 End critical point:  $\frac{7}{3}$

9. Graph two periods  $y = 4 \csc\left(2\theta - \frac{\pi}{2}\right) - 10 = 4 \csc\left(2\left(\theta - \frac{\pi}{4}\right)\right) - 10$



Amplitude: 4  
 for  $\sin$   
 Sinusoidal axis:  $y = -10$   
 Period:  $\frac{2\pi}{2} = \pi$   
 Phase shift:  $\frac{\pi}{4}$   
 End critical point:  $\frac{5\pi}{4}$