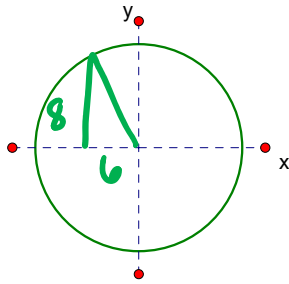


Algebra 2 H  
Pythagorean Identities

Name:

1. For the rotation angle  $\theta$  with terminal point  $(-6, 8)$ , write the six trig ratios for  $\theta$ .



$$\begin{aligned} \sin\theta &= \frac{4}{5} & \csc\theta &= \frac{5}{4} \\ \cos\theta &= \frac{-3}{5} & \sec\theta &= \frac{-5}{3} \\ \tan\theta &= \frac{-4}{3} & \cot\theta &= \frac{-3}{4} \end{aligned}$$

Calculate this very famous Pythagorean identity:  $(\sin\theta)^2 + (\cos\theta)^2$

$$\left(\frac{4}{5}\right)^2 + \left(\frac{-3}{5}\right)^2 = \frac{16}{25} + \frac{9}{25} = \frac{25}{25} = 1$$

Other Pythagorean identities:

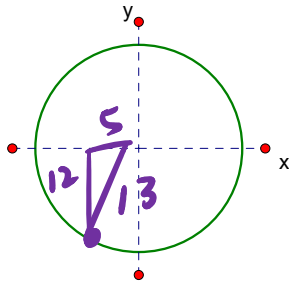
$$1 + \cot^2 \theta = \csc^2 \theta$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

\*Notice how we move the square operation to after the ratio instead of after the  $\theta$ ? Why do you think we write it this way?

*we are not squaring the  $\theta$ , we are squaring the ratio!*

2. For the rotation angle  $\theta$  with terminal point  $(-5, -12)$ , write the six trig ratios for  $\theta$ .



$$\begin{aligned} \sin\theta &= \frac{-12}{13} & \csc\theta &= \frac{-13}{12} \\ \cos\theta &= \frac{-5}{13} & \sec\theta &= \frac{-13}{5} \\ \tan\theta &= \frac{12}{5} & \cot\theta &= \frac{5}{12} \end{aligned}$$

Verify the three Pythagorean identities using algebra:

$$\star \left(\frac{-12}{13}\right)^2 + \left(\frac{-5}{13}\right)^2 = \frac{144}{169} + \frac{25}{169} = 1 \quad \checkmark$$

$$\star 1 + \left(\frac{5}{12}\right)^2 = \left(\frac{-13}{12}\right)^2$$

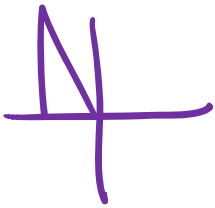
$$1 + \frac{25}{144} = \frac{169}{144} \quad \checkmark$$

$$\star \left(\frac{12}{5}\right)^2 + 1 = \left(\frac{-13}{5}\right)^2 \quad \frac{144}{25} + 1 = \frac{169}{25} \quad \checkmark$$

Evaluate the following using exact values:

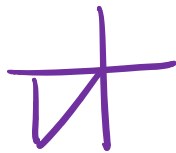
3.  $\cos 480^\circ$

$$\cos 120^\circ = -\frac{1}{2}$$



4.  $\sin 585^\circ$

$$\sin 225^\circ = -\frac{\sqrt{2}}{2}$$



5.  $\tan(-600^\circ)$

$$\tan(-240^\circ) = \tan 120^\circ = -\sqrt{3}$$

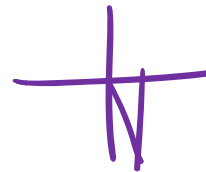


6.  $\sin 450^\circ$

$$2\pi = \frac{6\pi}{3}$$

10.  $\cos \frac{11\pi}{3}$

$$\cos \frac{5\pi}{3} = \frac{1}{2}$$



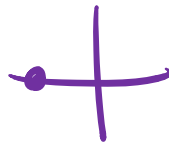
7.  $\cos(-2520^\circ)$

$$\cos 0^\circ = 1$$

8.  $\tan 855^\circ$

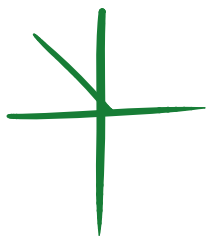
9.  $\sin 7\pi$

$$\sin \pi = 0$$



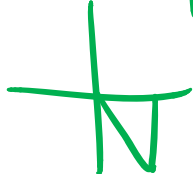
11.  $\tan\left(-\frac{13\pi}{4}\right)$

$$= -1$$



12.  $\sin\left(\frac{15\pi}{4}\right)$

$$\sin \frac{7\pi}{4} = -\frac{\sqrt{2}}{2}$$

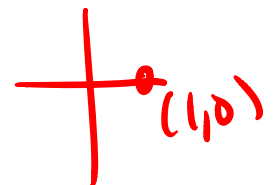


13.  $\cos\left(\frac{23\pi}{6}\right)$

$$= \frac{\sqrt{3}}{2}$$



14.  $\cot 10\pi$



Evaluate the following:

15.  $\frac{2(\sin 30^\circ) \cdot (\cos 45^\circ)}{8}$

$$\frac{2 \cdot \frac{1}{2} \cdot \frac{\sqrt{2}}{2}}{8} = \frac{\frac{\sqrt{2}}{2}}{8} = \frac{\sqrt{2}}{2} \cdot \frac{1}{8} = \frac{\sqrt{2}}{16}$$

16.  $\frac{3(\sin 60^\circ) \cdot (\cos 135^\circ)}{(\sin 30^\circ)}$

$$\frac{3 \cdot \frac{\sqrt{3}}{2} \cdot -\frac{\sqrt{2}}{2}}{\frac{1}{2}} = \frac{-3\sqrt{6}}{4} \cdot 2 = -\frac{3\sqrt{6}}{2}$$

17.  $5 \sin \frac{\pi}{2} + 4 \tan \frac{5\pi}{4} - 3 \cos \pi$

$$5 \cdot 1 + 4 \cdot 1 - 3 \cdot -1 = 12$$

18.  $\frac{\left(\cos \frac{4\pi}{3}\right)}{\left(\sin \frac{5\pi}{6}\right) - \left(\sin \frac{11\pi}{6}\right)}$

$$= \frac{-\frac{1}{2}}{\frac{1}{2} + \frac{1}{2}} = -\frac{1}{2}$$